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Optimizing Service Selection for Probabilistic QoS Attributes

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Abstract. The service selection problem (SSP) – i.e., choosing from sets of functionally equivalent services in order to fulfill certain business process steps based on non-functional requirements – has frequently been addressed in literature considering deterministic values for the Quality of Service (QoS) attributes. However, the usage of deterministic values does not reflect the uncertainty about the actual value of an attribute during execution, thus ignoring the risk of QoS violations. In the paper at hand, a simulative step, based on stochastic QoS attributes, is performed as complement for optimally solving the SSP using linear programming methods. With this two-step approach, uncertainties in the selected set of services can be explicitly revealed and addressed through repeated selection steps, thus allowing to prevent the violation of QoS restrictions much more effectively.

Introduction 1

In Service-oriented Architectures (SOA), business processes can be realized by composing loosely coupled services. Depending on their granularity, these services provide a more or less complex functionality [1]. Thereby, the services are not necessarily located only within the boundaries of the own enterprise. In the *Internet of Services*, multiple service providers offer their services at various service marketplaces [2]. If services with substitutable functionalities are available at different cost and quality levels, service requesters have the opportunity to decide which services from which service providers to select, based on their preferences regarding Quality of Service (QoS). This service selection problem (SSP) respectively its solution recently attracted a lot of attention in the literature [3–6].

In this problem, an abstract representation of a workflow is assumed to be given (e.g., in Business Process Modeling Notation – BPMN), as well as a list of functionally equivalent services which are able to accomplish the tasks of the respective workflow steps. The aim is to assign each workflow step exactly one service from the respective set of functionally equivalent candidate services, so that the overall (workflow) QoS is optimized and the requesters' end-to-end QoS requirements are satisfied. In order to compute an (optimal) solution, almost

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exclusively deterministic values for the QoS attributes are considered at planning time in the literature. However, these values do not reflect the uncertainty that is associated with an attribute during execution. E.g., response times – i.e. the elapsed time period between the service invocation to the response arrival – may fluctuate due to varying network or computational load, thus resulting in a violation of the requester's QoS requirements in the actual workflow execution.

Therefore, we propose to perform an additional simulation step that takes stochastic distributions for the QoS attributes into account after having computed the optimal solution to the SSP (considering only deterministic values). This simulation step allows to detect potential violations of QoS restrictions in the actual execution, based on the respective probability of such events. Depending on the requester's preferences, the outcome of the simulation may trigger repeated optimization steps using additional restrictions. As a proof-of-concept, we implemented and evaluated a simulation for the QoS attribute response time.

The remainder of this work is structured as follows: In Section 2, we will present our approach for optimally solving the SSP using linear programming, based on deterministic QoS values. In Section 3, the potential drawbacks of deterministic optimization will be outlined. Based on the findings, a simulation process that relies on stochastic QoS attributes will be presented and evaluated using a prototypical tool. The paper closes with a conclusion and an outlook of our future work in Section 4.

2 Optimal Service Selection for Complex Workflows

In this section, we present our approach for the computation of an optimal solution to the SSP. For this, we formulate a linear optimization problem, which can be solved optimally – if a solution exists – using (mixed) integer linear programming (MILP) techniques from the field of operations research [7]. The optimization problem consists of a target function and a set of constraints. We perform a worst-case analysis – instead of an average-case analysis – by applying our aggregation functions proposed in [8] in order to make sure that all restrictions are satisfied at planning time. Performing an average-case analysis would have led to a solution, where the restrictions are satisfied only *in average*.

For the optimization, we consider the QoS attributes response time e (elapsed time from the service invocation until the response arrival), costs c (costs for the invocation of a service), reliability r (the probability that the service successfully provides the requested results), and throughput d (number of parallel service invocations), although the mentioned simulation step will only be performed for response time e. With these QoS attributes – in fact with a subset of these attributes – the aggregation types summation, multiplication and the min/max operator are covered. The integration of further aggregation types is straightforward.

In the paper at hand, we concentrate on the workflow patterns sequence, parallel split (AND-split), synchronization (AND-join), exclusive choice (XOR-split), simple merge (XOR-join), and arbitrary cycles (Loop), which only form a

subset of all workflow patterns (cf. [9]). The patterns can be combined to create complex workflows. An example for such a complex workflow is given in Figure 1.

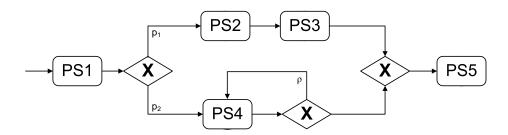


Fig. 1: Example abstract workflow

We consider an abstract workflow (e.g., in BPMN), consisting of n tasks respectively process steps PS_i . For each PS_i with $i \in I = \{1, ..., n\}$, a set J_i of m_i services $j_i \in J_i = \{1, ..., m_i\}$, able to realize PS_i , exists. Each process step PS_i thereby is realized by exactly one service j_i . This is indicated by the demand for (binary) decision variables $x_{ij} \in \{0,1\}$ (cf. condition (14)). The logical order of the process steps is depicted from the abstract workflow as follows: in case PS_k is a direct successor of PS_i , we add $PS_i \to PS_k$ to a set $DS = \{PS_i \to PS_k | PS_k | \text{direct successor of } PS_i\}$. DS_s is the set of start tasks, i.e., the tasks that need to be executed first in the workflow. In addition, we define DS_e as the set of end tasks, i.e., tasks with no direct successor. To give an example, we refer to Figure 1. Here, PS_3 is a direct successor of PS_2 . We therefore add $PS_2 \to PS_3$ to DS.

With respect to XOR-splits and XOR-joins, we define a set $L = \{1, ..., o\}$ of o path numbers for the paths within the XOR-split and -join – and name these paths XOR-paths. Thereby, $l \in L$ represents the respective XOR-path number. The process steps PS_{i_l} within an XOR-path are assigned to a set W_l , $PS_{i_l} \in W_l = \{PS_i | PS_i \text{ in XOR-path } l\}$, and their respective process step numbers i_l are assigned to the set IW_l , $i_l \in IW_l = \{i | PS_i \in W_l\}$. Further, $S = \{PS_1, ..., PS_n\} \setminus (W_1 \vee ... \vee W_o)$ represents a set of the remaining process steps PS_i when removing process steps PS_{i_l} from a set of all process steps. $IS = I \setminus (IW_1 \vee ... \vee IW_o)$ denotes the set of the corresponding process step numbers.

Within an XOR-path, we assume a sequential arrangement of the process steps and label the first and last process steps with $PS^1_{i_1}$ and $PS^e_{i_1}$. The respective start times for these process steps are labeled analogously with $t^1_{i_l}$ and $t^e_{i_l}$. The probability that XOR-path l is executed, is indicated by p_l . We demand $\sum_{l=1}^o p_l = 1$.

Regarding the workflow pattern Loop, I_{loop} represents the set of process step numbers i with a Loop. Further, ρ_i denotes the respective probability that this Loop is followed (cf. PS_4 in Figure 1). Thereby, ρ is independent of whether the Loop was followed or not before. If a Loop is followed multiple times, the

respective process steps are executed multiple times, too. As this affects the regarded, aggregated QoS values, we define e_{ij}^* in (1), c_{ij}^* in (2), and r_{ij}^* in (3) in dependence of a boundary value consideration of ρ (cf. [8]). The throughput d_{ij} is not effected by a Loop.

$$e_{ij}^* := \begin{cases} \frac{1}{1-\rho_i} e_{ij} &, \text{ if } i \in I_{loop} \\ e_{ij} &, \text{ else} \end{cases}$$
 (1)

$$c_{ij}^* := \begin{cases} \frac{1}{1-\rho_i} c_{ij} &, \text{ if } i \in I_{loop} \\ c_{ij} &, \text{ else} \end{cases}$$
 (2)

$$r_{ij}^* := \begin{cases} \frac{(1-\rho_i)r_{ij}}{1-\rho_i r_{ij}} & , \text{ if } i \in I_{loop} \\ r_{ij} & , \text{ else} \end{cases}$$
 (3)

Based on our aggregation functions in [8], we propose Model 1 to perform the proposed worst-case analysis. Here, QoS restrictions are labeled with b (bounds).

Model 1 Optimization Problem

Objective Function

minimize
$$F(x) = \sum_{i \in I} \sum_{j \in J_i} c_{ij}^* x_{ij}$$
 (4)

s.t.

$$t_i = 0 \forall i \in I | PS_i \in DS_s (5)$$

$$t_i + \sum_{j \in J_i} e_{ij}^* x_{ij} \le t_k \qquad \forall i \in I | PS_i \to PS_k \in DS$$
 (6)

$$t_i + \sum_{j \in J_i} e_{ij}^* x_{ij} \le b_e \qquad \forall i \in I | PS_i \in DS_e$$
 (7)

$$t_{i} + \sum_{j \in J_{i}} e_{ij}^{*} x_{ij} \leq t_{k} \qquad \forall i \in I | PS_{i} \to PS_{k} \in DS$$

$$t_{i} + \sum_{j \in J_{i}} e_{ij}^{*} x_{ij} \leq b_{e} \qquad \forall i \in I | PS_{i} \in DS_{e}$$

$$\max_{l \in L} \{ (t_{i_{l}}^{1} + \sum_{i \in IW_{l}} \sum_{j \in J_{i}} e_{ij}^{*} x_{ij}) \} \leq t_{k} \qquad \forall i \in I | PS_{i_{l}}^{e} \to PS_{k} \in DS$$

$$(8)$$

$$\max_{l \in L} \{ (t_{i_l}^1 + \sum_{i \in IW_l} \sum_{i \in I_i} e_{ij}^* x_{ij}) \} \le b_e \qquad \forall i \in I | PS_{i_l}^e \in W_l$$
 (9)

$$\sum_{i \in IS} \sum_{j \in J_i} c_{ij}^* x_{ij} + \max_{l \in L} \left\{ \sum_{i \in IW_l} \sum_{j \in J_i} c_{ij}^* x_{ij} \right\} \le b_c \tag{10}$$

$$\left(\prod_{i \in IS} \sum_{j \in J_i} r_{ij}^* x_{ij}\right) \cdot \left(\min_{l \in L} \left\{ \left(\prod_{i \in IW_l} \sum_{j \in J_i} r_{ij}^* x_{ij}\right) \right\} \right) \ge b_r \tag{11}$$

$$\sum_{i \in I} x_{ij} = 1 \qquad \forall i \in I \tag{13}$$

$$x_{ij} \in \{0, 1\} \qquad \forall i \in I, \forall j \in J_i$$
 (14)

Regarding Model 1, it has to be noted that the workflow patterns AND-split and AND-join are already covered in (8) to (12) (cf. [8]).

To compute an optimal solution using MILP techniques, a linear optimization problem is required. As the min/max operator as well as the multiplication are non-linear aggregation types regarding the decision variables x_{ij} , we apply the approximation (15) to (11) – which is very accurate for values z_{ij} close to 1 (like reliability) [10] – and exchange constraints (8)–(12) for (16)–(20). To explain this (second adaptation step), it has to be noted that if the minimum (maximum) of a set of values has to be higher (lower) or equal to a certain bound, each element of this set needs to satisfy this constraint.

$$\prod_{i=1}^{n} \sum_{j=1}^{m_i} z_{ij} x_{ij} \approx 1 - \sum_{i=1}^{n} (1 - \sum_{j=1}^{m_i} z_{ij} x_{ij})$$
(15)

$$t_{i_l}^1 + \sum_{i \in IW_l} \sum_{j \in J_i} e_{ij}^* x_{ij} \le t_k \qquad \forall l \in L, \forall i \in I | PS_{i_l}^e \to PS_k \in DS$$
 (16)

$$t_{i_l}^1 + \sum_{i \in IW_l} \sum_{j \in J_i} e_{ij}^* x_{ij} \le b_e \qquad \forall l \in L, \forall i \in I | PS_{i_l}^e \in W_l$$
 (17)

$$\sum_{i:(IS \vee IW_i)} \sum_{j \in J_i} c_{ij}^* x_{ij} \le b_c \qquad \forall l \in L$$
 (18)

$$\sum_{i \in IW_l} \sum_{j \in J_i} \sum_{i \in (IS \vee IW_l)} \sum_{j \in J_i} c_{ij}^* x_{ij} \le b_c \qquad \forall l \in L \qquad (18)$$

$$1 - \sum_{i \in (IS \vee IW_l)} (1 - \sum_{j \in J_i} r_{ij}^* x_{ij}) \ge b_r \qquad \forall l \in L \qquad (19)$$

$$\min_{i \in I} \{ \sum_{j \in J_i} d_{ij} x_{ij} \} \ge b_d \qquad (20)$$
aducted these substitutions, an optimal solution can be obtained

$$\min_{i \in I} \{ \sum_{j \in J_i} d_{ij} x_{ij} \} \ge b_d \tag{20}$$

Having conducted these substitutions, an optimal solution can be obtained by applying MILP techniques.

3 Stochastic Simulation of Complex Workflows

In the previous section, we have outlined how an optimal set of services can be selected for the process steps in a complex workflow, based on given QoS constraints. Because the underlying optimization problem is solved using MILP, the usage of deterministic QoS attributes is required. These fixed values commonly represent a lower or upper bound that is guaranteed by a service provider with respect to a certain QoS attribute in terms of a Service Level Agreement (SLA).

However, the usage of deterministic values does not reflect the uncertainty (or risk, which we use as a synonym) that may be associated with QoS attributes. Response time, e.g., is ultimately a stochastic variable that depends on various random determinants, such as network and computational load. Consider two sets of services for the same business process, where the second set has a slightly higher average response time for each service. However, the variance in response time is much lower for the second set, e.g., due to the usage of load-balancing techniques. While the first set is optimal with respect to the objective of minimal (average) response time, it exhibits a much more fluctuating behavior with respect to this attribute. This may lead to an increased risk of exceeding certain reponse times threshold, which is undesired. Thus, we believe that the notion of optimality

in service selection needs to regard two aspects: the average outcome of an QoS attribute as well as its fluctuation.

Accordingly, we propose to extend the representation and computation of QoS attributes in a manner that appropriately incorporates uncertainty. Our approach adapts a methodology suggested by Dawson and Dawson in the domain of project planning [11]. They introduce the notion of generalized activity networks [12]. Such networks consist of nodes and edges. Nodes represent activities (or tasks); edges represent precedence relationships and thus paths between the activities, where each task may have one or more incoming and outgoing incident edges. For additional details and an example, we refer to Dawson and Dawson [12]. Notably, the duration for each activity is given as stochastic distribution, rather than a deterministic value, in generalized activity networks. This is a well-known principle that has been applied in traditional planning techniques, such as PERT, which was devised in the early 1960s [13]. Furthermore, if more than one edge results from an activity, all edges are annotated with an execution probability. These execution probabilities may also be correlated between edges.

Following the findings by Schonberger [14], who states that traditional planning techniques such as PERT commonly underestimate the overall duration of an activity network, Dawson and Dawson utilize simulation as a means of analyzing generalized activity networks [11]. I.e., the activity network is virtually executed a selected number of times; in this process, the duration of each activity and choice of path execution is drawn as a random variable. The individual durations of all executed activities are then aggregated into an overall duration in each iteration. From the distribution of aforementioned overall durations, conclusions can be drawn about the characteristic of the activity network in actual execution. Most importantly, the probability that a set of activities exceeds a certain threshold due to the fluctuations in duration can be inferred.

The notion of generalized activity networks can easily be transferred to work-flows as a special application domain. In this scenario, services then correspond to activities, while splits (joins) constitute dummy activities with multiple outgoing (incoming) edges. Depending on the type of split (AND, XOR, or Loop), the execution probabilities of the edges and respective correlations will differ. E.g., in the case of AND-splits, each edge will be assigned a probability of 1, due to the fact that each edge is certainly executed.

Because services have multiple non-functional attributes, we not only adapt, but also extend Dawson and Dawson's approach. Namely, we allow for an *arbitrary* number of random variables, representing QoS attributes, being associated with each activity (i.e. service) apart from duration (which, in the context of workflows respectively services, translates into response time). In our proposed methodology, each QoS attribute for each service is modeled as an independent random variable adhering to some probability distribution. This loosely relates to the idea of *soft contracts* in Web service orchestration, as proposed by Rosario et al. [15].

The probability distribution may essentially be determined in two ways. The first option is to infer it, based on historic execution data of a service. This requires the installation of proper monitoring mechanisms. After a relevant sample has

been collected, a QoS attribute such as response time may, e.g., be represented through a normal distribution. The second option is that a service provider explicitly specifies a probability distribution for each QoS attribute.

In order to infer execution probabilities for each path, three options exist. The first is mining from historical data again. However, this requires that a workflow (or at least a workflow segment) that is identical to one being simulated has previously been executed and monitored. The second option is to have an user manually assign the probabilities, based on his or her knowledge about the underlying business process. The third and final option is to utilize conservative default values, assuming that either each path (in case of AND-splits) or the worst path with respect to each individual QoS attribute (XOR-splits) will be executed.

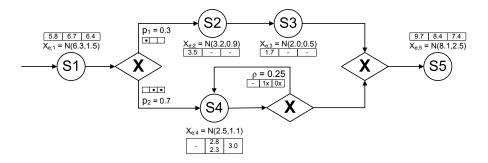


Fig. 2: Example workflow including simulation outcomes

Figure 2 depicts an example workflow for which a set of services (S1 through S5) has been selected. It addition, the random variables and respective probability distributions for each service, as well as execution probabilities for each edge, are illustrated. For reasons of simplicity, solely the random variables for the QoS attribute response time are included. For service S1, e.g., the response time is given by $X_{e;1}$, which is normally distributed (N) with a mean value of 6.3 seconds and a standard deviation of 1.5 seconds. For the XOR-split, the probability of executing the top and bottom path is 0.3 and 0.7 respectively. Accordingly, for the Loop construct, the probability of looping and thus repeatedly executing S4 is 0.25.

Figure 2 further depicts three exemplary simulation runs for the sample workflow. For every service, the randomly drawn response times are depicted in the boxes next to the random variables. For the XOR-split, the pursued path is indicated by a bullet; for the Loop construct, the number of additional executions (repetitions) of S4 is depicted. As can be seen, each run results in a different outcome for each service with respect to response time and in varying paths being executed. E.g., in the first iteration in the example, services S1, S2, S3, and S5 have response times of 5.8, 3.5, 1.7, and 9.7 seconds respectively. The lower path

is not executed, and thus, S4 and the consecutive Loop construct are omitted. Accordingly, the overall response time for the first iteration is 20.7 seconds (and 20.2 and 16.8 seconds for the second and third iteration respectively). Once the process is repeated multiple times, a representative distribution for each QoS attribute can be obtained.

Service selection and workflow simulation serve as a mutual complement: In the first step, a set of services is selected by solving a linear optimization problem. This provides an optimal result with respect to the objective of minimizing total cost and allows to make statements about the workflow characteristics in theory. In the second step, the resulting workflow is simulated, ideally based on historic execution data, which allows to anticipate the workflow characteristics in practical execution. If the uncertainty in the workflow is found to be unacceptable with respect to given constraints, the selected set of services is discarded. This may, e.g., be the case if a specified response time constraint is not met with a certain probability. Consecutively, the process of computing an optimal solution is repeated with further restrictions. A manifest strategy is to explicitly exclude one or more services with the highest standard deviation in a critical QoS attribute from the set of candidate services.

To assess the principal benefits and effectiveness of our approach, we have implemented a prototypical workflow simulation tool in Java. The tool allows to specify complex workflows, consisting of services and their structure, using an XML-based format¹. For each service, an arbitrary number of QoS attributes, along with the respective probability distributions, may be specified and freely parameterized.

A simulation with one million iterations has been conducted for the example workflow in Figure 2 using the aforementioned tool. Additionally, the workflow has been modified for a second simulation. In detail, the mean of the response time probability distribution for each service was incremented by 0.2 seconds, and the standard deviation was set to half of its original value. I.e., each initially selected service has been replaced by a variant that is less optimal on average, but also shows less fluctuation in terms of response time. In practice, this process would be iteratively conducted for one service at a time.

The resulting distributions of the workflows' overall response times are depicted in Figure 3, where the absolute frequency refers to clusters (or classes) of outcomes that were identical up to the first decimal place. While the modified workflow responds slower on average, it can be seen that it is significantly more favorable once a strict response time constraint of approximately 20 seconds or more has been specified. This figure is fairly close to the average response time of 18.2 and 18.9 seconds for the original and modified workflow respectively. In these cases, the original workflow is much more likely to break the constraint than the modified workflow. E.g., a response time restriction of 22.5 seconds is violated with a probability of 11.15% by the original workflow – for the modified workflow, the probability is only 6.25%, i.e. roughly half. Differently stated, an increase

¹ A sample listing is available from http://www.kom.tu-darmstadt.de/~lampeu/icsoft-2010/workflow.xml

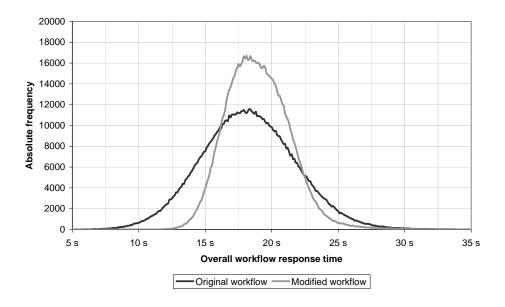


Fig. 3: Distribution of the overall response time for two workflows

in average response time (and cost) is traded against a decrease in uncertainty – namely of breaking an overall response time constraint – by replacing the original services through their alternative counterparts.

4 Conclusion

In the work at hand, we have presented two complimentary approaches to the problem of QoS-aware service selection for complex workflows. As foundation, we have outlined how an optimal set of services can be identified under given QoS constraints using linear programming. However, this process is based on deterministic values, which insufficiently reflect the uncertainty associated with a QoS attribute in actual execution. E.g., response times may heavily fluctuate due to network and computational load, thus leading to QoS violations in the actual execution of a workflow.

As a solution, we have adapted an existing methodology for the simulation of generalized activity networks to the specific field of workflows in SOA. This simulation process allows to assess the expected characteristics of a workflow, most importantly the likelihood that a QoS constraint will be violated, in more detail. Depending on a requester's preferences, the outcome of the simulation process can be utilized to repeatedly conduct the service selection procedure, thus minimizing the probability of QoS violations more effectively. The practical applicability and benefit of our approach has been proven using a prototypical implementation of a workflow simulation tool.

In our future work, we aim at combining the currently separated steps of service selection and workflow simulation into an integrated tool. We will further investigate the issue of mining probability distributions from historic service execution data as a prerequisite of more realistic simulation. In this context, QoS attributes besides response time will also be explicitly addressed.

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